


Quiz 10
Chemical Engineering Thermodynamics
March 28, 2019

Determine the fugacity (MPa) for n-pentane at (a) 350 K and 0.1 MPa and (b) 350 K and 0.8 MPa using the virial equation and the shortcut vapor pressure. (c) *First use PREOS.xls to calculate the saturated vapor pressure, and the fugacity's for "a" and "b". Put your answers in the chart on page 2 below. (Show your work, i.e. write the equations with values, units and answers.)*

$T_c = 470 \text{ K}$, $P_c = 3.37 \text{ MPa}$, $V_c = 356 \text{ cm}^3/\text{mole}$, $\omega = 0.249$, $R = 8.31 \text{ J}/(\text{mole K}) = 8.31 \text{ cm}^3\text{MPa}/(\text{mole K})$

Determine if the short cut method is appropriate.
 Calculate the vapor pressure and determine the state for each condition.
 Determine if the virial equation is appropriate.
 Calculate the fugacity (using different methods for the different states).

$$\log_{10} P_r^{sat} = \frac{7}{3}(1 + \omega)\left(1 - \frac{1}{T_r}\right)$$

9.11  Shortcut vapor pressure equation. Use care with the shortcut equation below $T_r = 0.5$.

$$\ln \phi = \frac{BP}{RT}$$

9.31

$Z = 1 + (B^0 + \omega B^1)P_r/T_r$ or $Z = 1 + BP/RT$	7.6
where $B(T) = (B^0 + \omega B^1)RT_c/P_c$	7.7
$B^0 = 0.083 - 0.422/T_r^{1.6}$	7.8
$B^1 = 0.139 - 0.172/T_r^{4.2}$	7.9
Subject to $T_r > 0.686 + 0.439P_r$ or $V_r > 2.0$	7.10

Poynting Correction

$$f = f^{sat} \exp\left(\frac{V^L(P - P^{sat})}{RT}\right)$$

$$V^{satL} = V_C Z_C^{(1-T_r)^{0.2857}}$$

$$Z_c = P_c V_c / (RT_c)$$

T	350K	350K	350K	350K
P	---	---	0.1 MPa	0.8 MPa
T_r , K	---	---		
P_r , MPa	---	---		
	P^{sat} , MPa	f^{sat} , MPa	f part a, MPa	f part b, MPa
PREOS.xls				
State				
Virial Eqn./ Shortcut M.				

T	350K	350K	350K	350K
P	---	---	0.1 MPa	0.8 MPa
T_r , K	---	---	0.745	0.745
P_r , MPa	---	---	0.0297	0.237
	P^{sat} , MPa	f^{sat} , MPa	$f^{\text{part a}}$, MPa	$f^{\text{part b}}$, MPa
PREOS.xls	0.340	0.309	0.0974	0.316
State	L/V	L/V	V	L
Virial Eqn./ Shortcut M.	0.339	0.308	0.0972	0.316

a)

Does SCM work? $T_r = 0.745 > 0.5$ **Yes**

$$P^{\text{sat}} = P_c 10^{(7/3 (1 + \omega)(1 - 1/T_r))} = 3.37 \text{ MPa } 10^{(7/3 (1 + 0.249)(1 - 1/0.745))} = 0.106 \text{ MPa}$$

Does Virial Eqn. Work?

$$T_r = 0.745 > 0.686 + 0.439P_r = 0.686 + (0.439) 0.0297 \text{ MPa} = 0.699 \text{ **Yes**}$$

$$B_0 = 0.083 - 0.422/T_r^{1.6} = -0.593$$

$$B_1 = 0.139 - 0.172/T_r^{4.2} = -0.453$$

$$B = (B_0 + \omega B_1)RT_c/P_c = -818 \text{ cm}^3/\text{mole}$$

$$f = P \exp(-818 \text{ cm}^3/\text{mole } 0.1 \text{ MPa} / (8.31 \text{ cm}^3 \text{ MPa} / (\text{K mole}) 350 \text{ K})) = \mathbf{0.0972 \text{ MPa}}$$

b) Get $f^{\text{sat}} = P^{\text{sat}} \exp(BP^{\text{sat}}/(RT^{\text{sat}}))$ if

$$T_r = 0.745 > 0.686 + 0.439P_r^{\text{sat}} = 0.686 + (0.439) 0.101 \text{ MPa} = 0.730 \text{ **Yes**}$$

$$f^{\text{sat}} = 0.339 \text{ MPa } \exp(-818 \text{ cm}^3/\text{mole } 0.339 \text{ MPa} / (8.31 \text{ MPa cm}^3 / (\text{mole K}) 350 \text{ K})) = 0.308 \text{ MPa}$$

$$V^{\text{L}} = V_c Z_c^{(1-T_r)^{0.2857}} = 356 \text{ cm}^3/\text{mole } 0.307^{(1-0.745)^{0.2857}} = 160 \text{ cm}^3/\text{mole}$$

$$Z_c = P_c V_c / (RT_c) = 3.37 \text{ MPa } 356 \text{ cm}^3/\text{mole} / (8.31 \text{ MPa cm}^3 / (\text{mole K}) 470 \text{ K}) = 0.307$$

$$f = f^{\text{sat}} \exp(160 \text{ cm}^3/\text{mole } (0.8 \text{ MPa} - 0.339 \text{ MPa}) / (8.31 \text{ MPa cm}^3 / (\text{mole K}) 350 \text{ K})) =$$